

RECENT STUDIES OF ELECTRON MOLECULE SCATTERING WITH THE R-MATRIX METHOD

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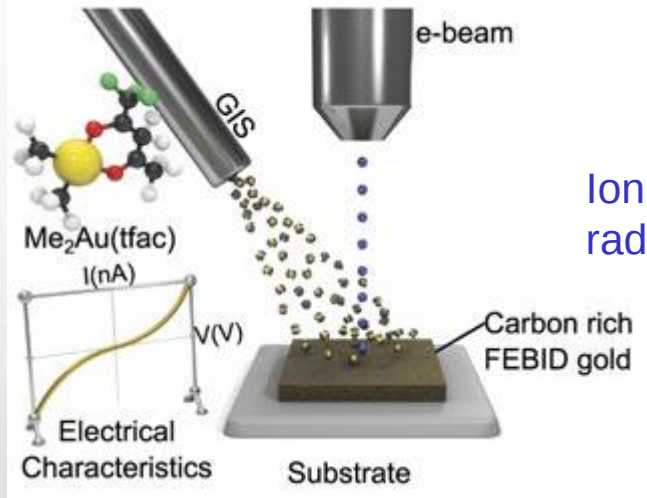


The Open University

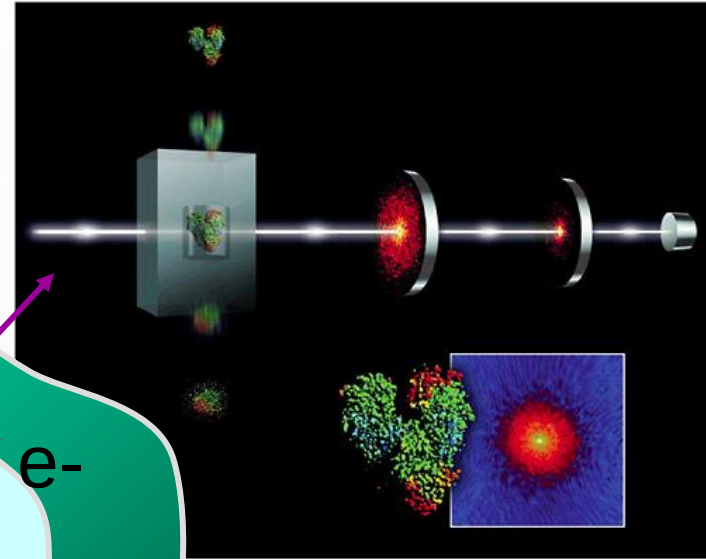
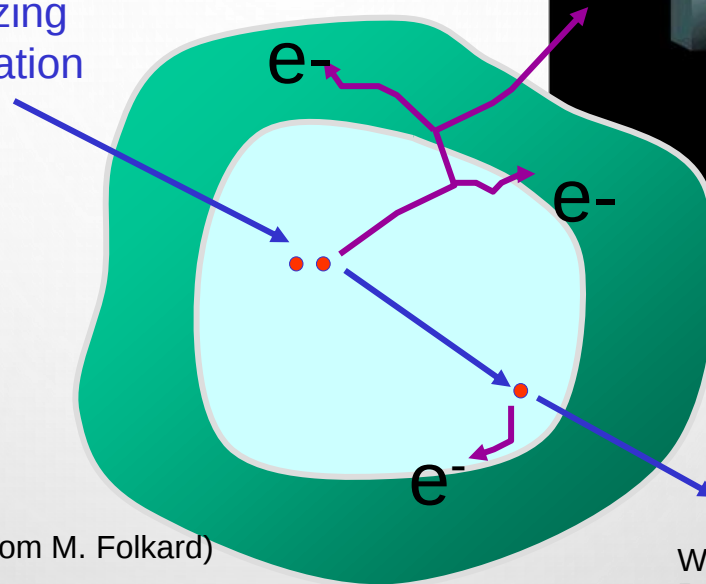
Electron-molecule collisions

Scientific Reports 6 (2016) 34003

Chapman, Lawrence Livermore
National Laboratory



Ionizing
radiation

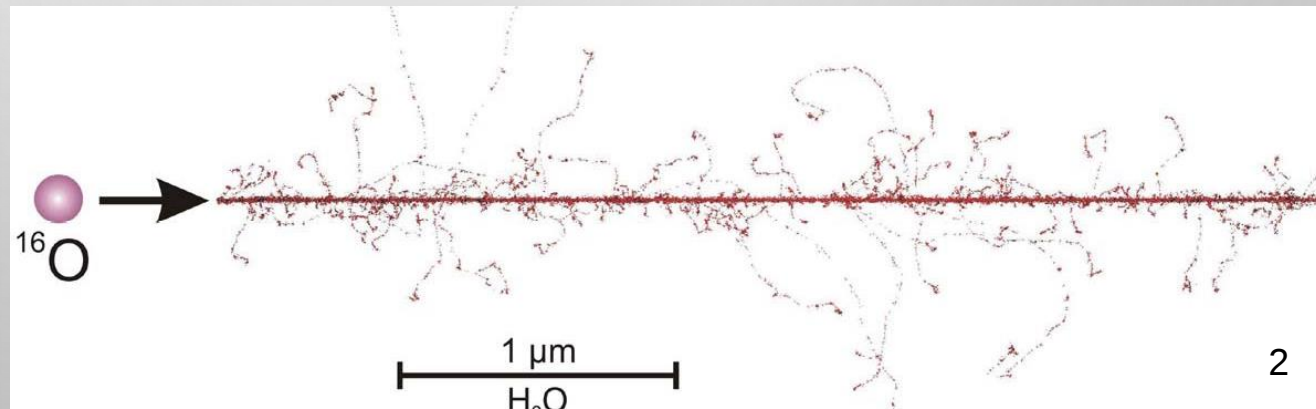


(Adapted from M. Folkard)

W. Friedland, GSF-Institute of Radiation
Protection . PARTRAC, MC simulation



Osaka University



Low energy electron-molecule collisions

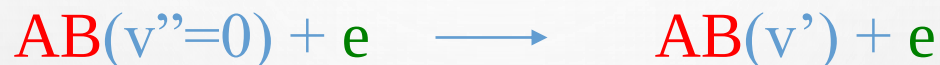
Elastic scattering



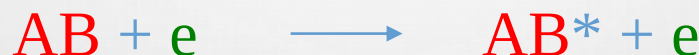
Rotational excitation



Vibrational excitation



Electronic excitation



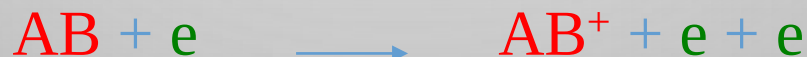
Dissociative electron attachment



Dissociative excitation*



Ionization

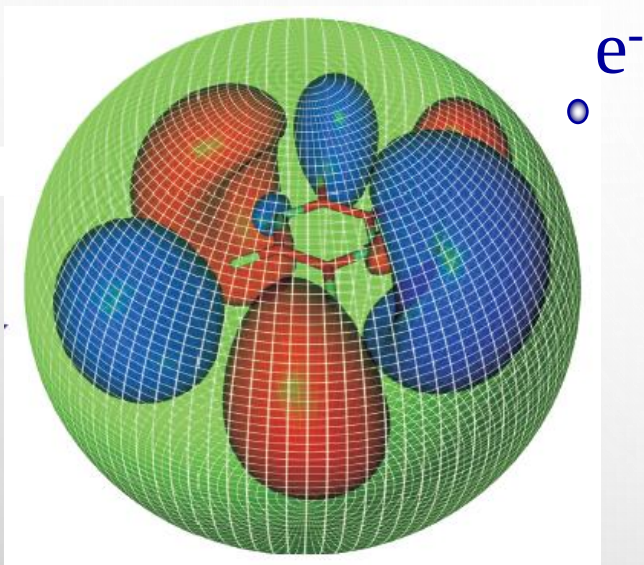


Energy

* Impact
dissociation

R-matrix method for e-molecule collisions

Fixed-Nuclei approximation: **neglect of nuclear motion**



R-matrix sphere of radius a

P. G. Burke, *R-Matrix Theory of Atomic Collisions: Application to Atomic, Molecular and Optical Processes* (Springer) 2011.

Inner region:

- exchange and correlation important
- explicitly multielectronic
- basis set methods
- multicentre expansion

Outer region:

- exchange negligible and 'correlation' very simple
- one explicit electron
- long-range multipolar interactions
- single centre expansion

R-matrix method for e-molecule collisions

Inner region: calculation of Ψ_k^{N+1} from diagonalization of $\mathbf{H}^{N+1}$

$$\Psi_k^{N+1} = \mathcal{A} \sum_{i,j} a_{i,j,k} \phi_i^N \eta_{i,j} + \sum_j b_{j,k} \phi_j^{N+1}$$

- Good description of **electronic molecular states** ϕ_i^N : **SA-CASSCF method**

$$\phi_i^N = \sum_{i,j} c_{i,j} \zeta_j^N$$

$$\zeta_j^N = \parallel \varphi_1 \varphi_2 \varphi_3 \dots \varphi_N \parallel$$

Limited by methodology, size of calculation and size of R-matrix sphere

- Good description of **correlation/polarization effects**: **choice of L^2 functions**
- Good description of **continuum** using **continuum orbitals** $\eta_{i,j}$: **use of GTOs, BTOs or both**

UKRmol+ suite

Time-independent approach
to low-energy
electron/positron scattering
and photoionization

Mašin et al, CPC, **249**, 107092 (2020)
<https://doi.org/10.1016/j.cpc.2019.107092>
arxiv.org/abs/1908.03018

Publication date:

January 15, 2021

DOI:

DOI [10.5281/zenodo.4442407](https://doi.org/10.5281/zenodo.4442407)

Keyword(s):

electron scattering, positron scattering, resonances, photoionization,

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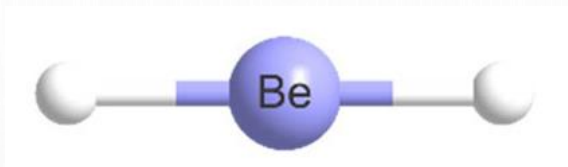
Versions

Version 3.1.1	Jan 15, 2021
10.5281/zenodo.4442407	
Version 3.1	Oct 23, 2020
10.5281/zenodo.4120705	
Version 3.0	Aug 19, 2019
10.5281/zenodo.3371125	
Version 2.0.5	Jun 28, 2019

<https://zenodo.org/>

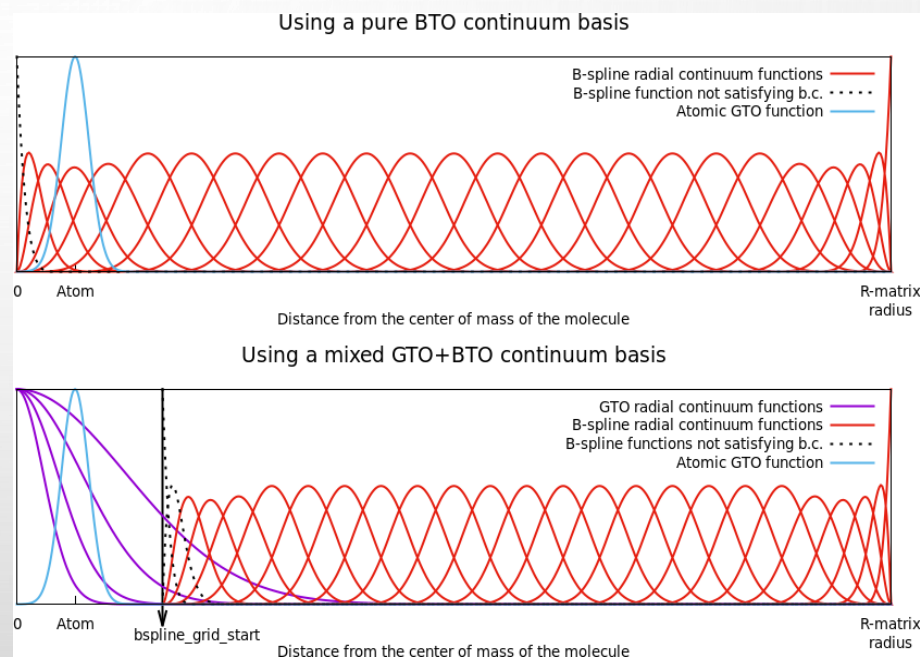
BeH₂: inelastic cross section and DCS

Present in plasma in divertors of thermonuclear fusion reactors (e.g. ITER)

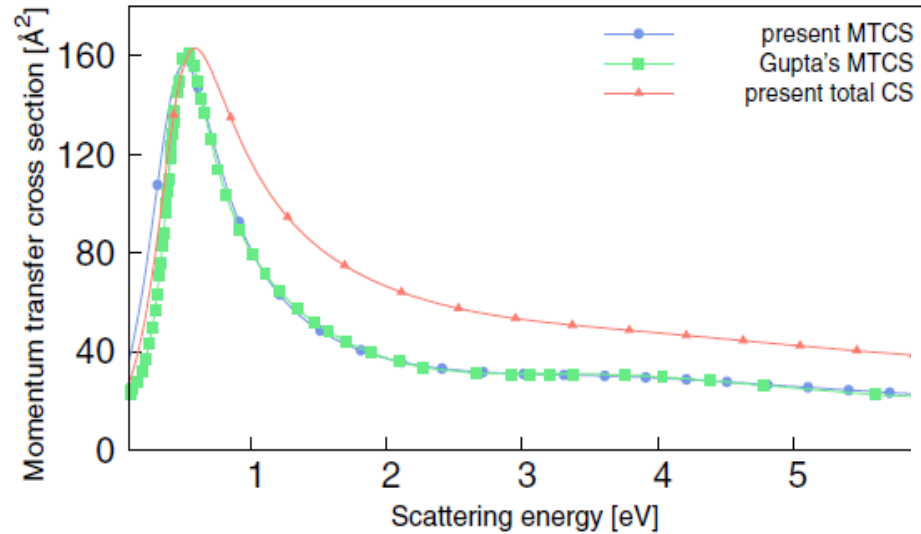


Small enough (and 6 e⁻) to use our best models:

- cc-pVDZ basis set (aug had little effect)
- CASSCF (4,14)
- 40 target states
- R-matrix radius = 15 a_0
- BTO-only continuum
- Max. partial wave $l=8$

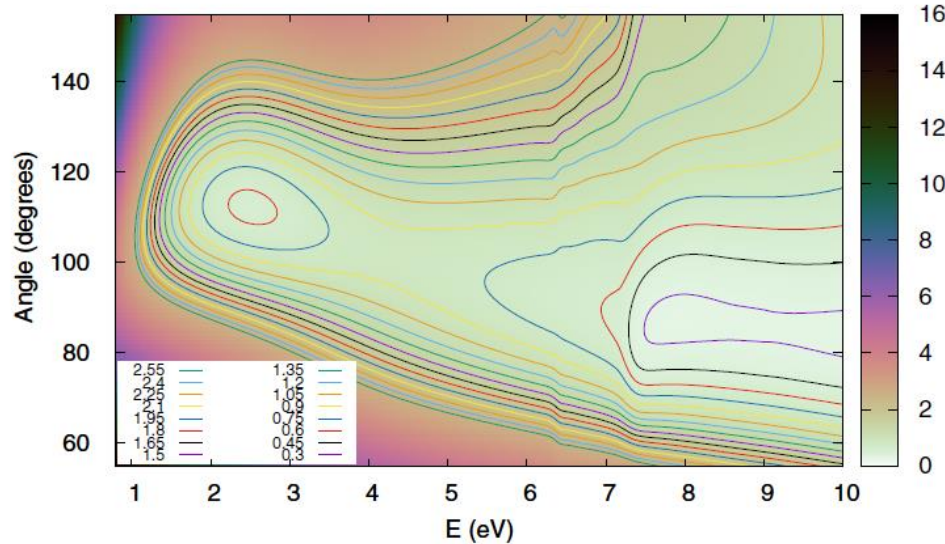


BeH₂: cross sections

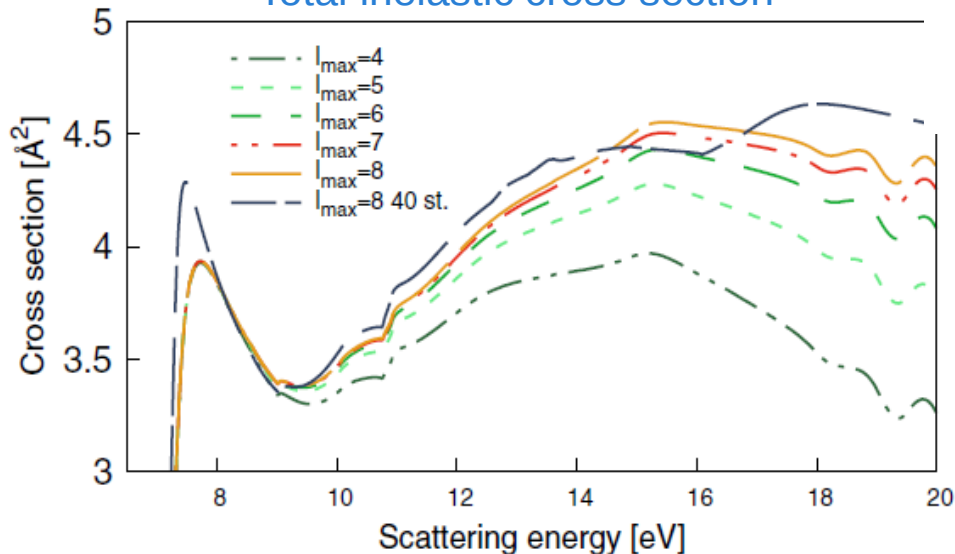


Total and momentum transfer cross section

Elastic DCS



Total inelastic cross section

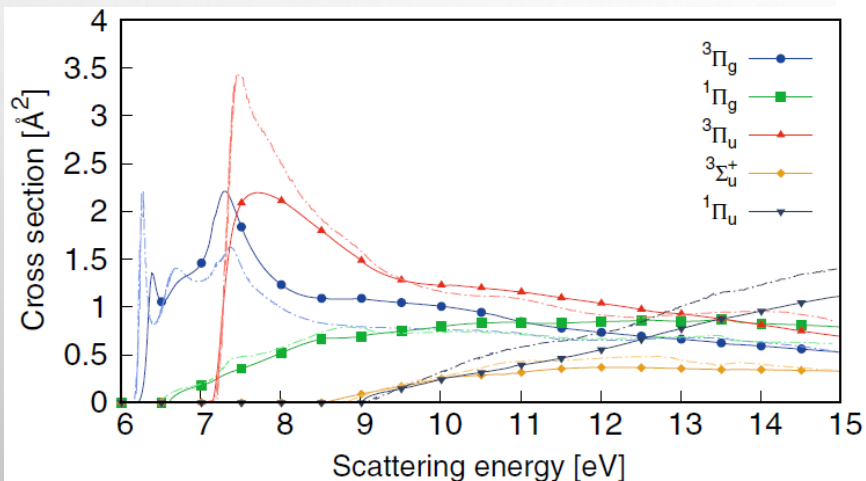


Effect of improved continuum and polarization description

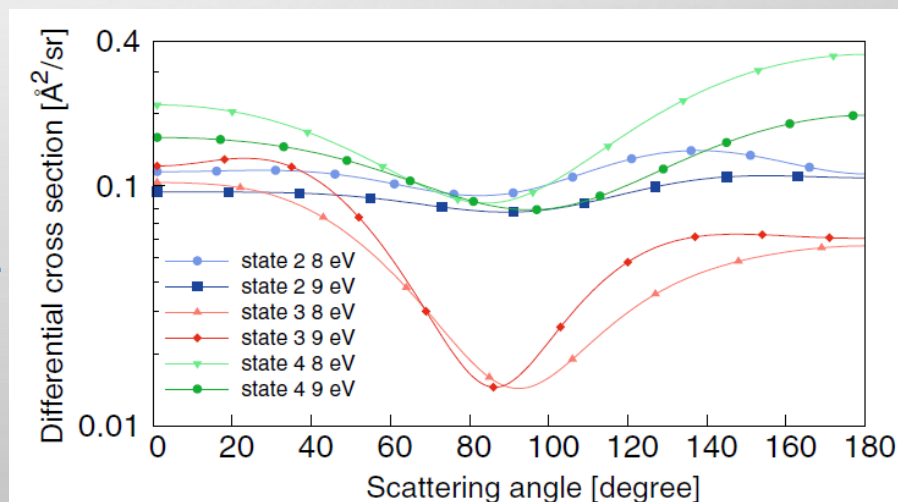
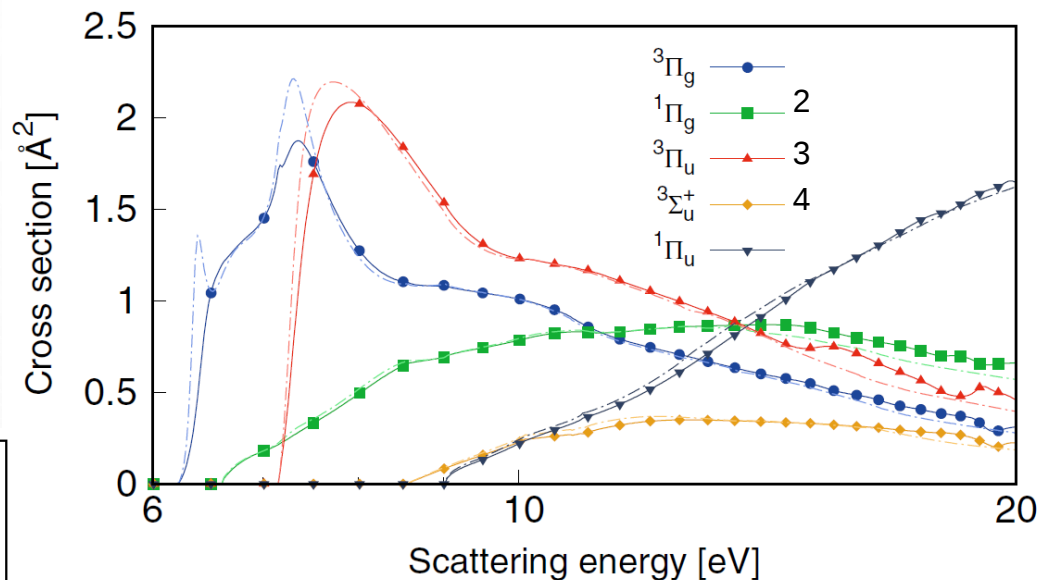
BeH₂: inelastic cross section and DCS

State-to-state integral cross sections: 14 (solid) vs. 40 (dashed) target states

Comparison with earlier (dashed) results

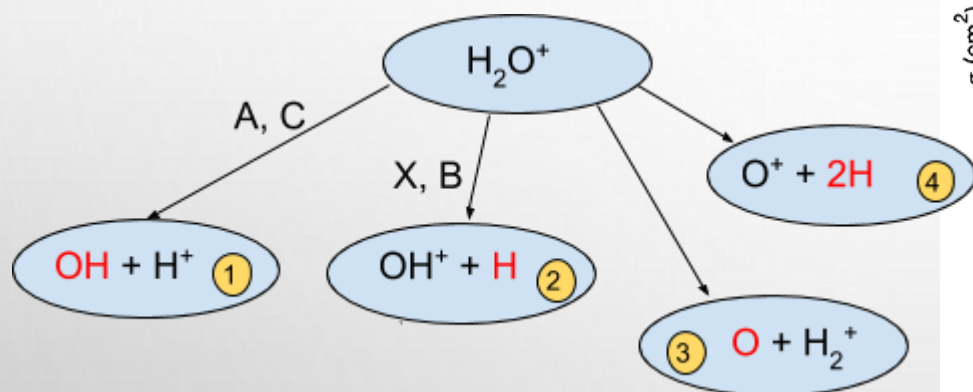
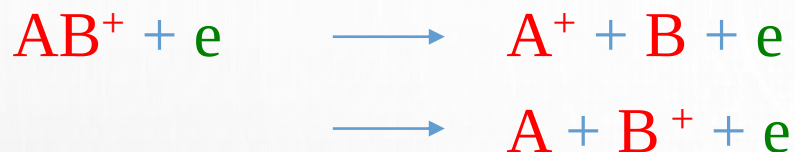


State-to-state DCS: expected behaviour for singlets and triplet states

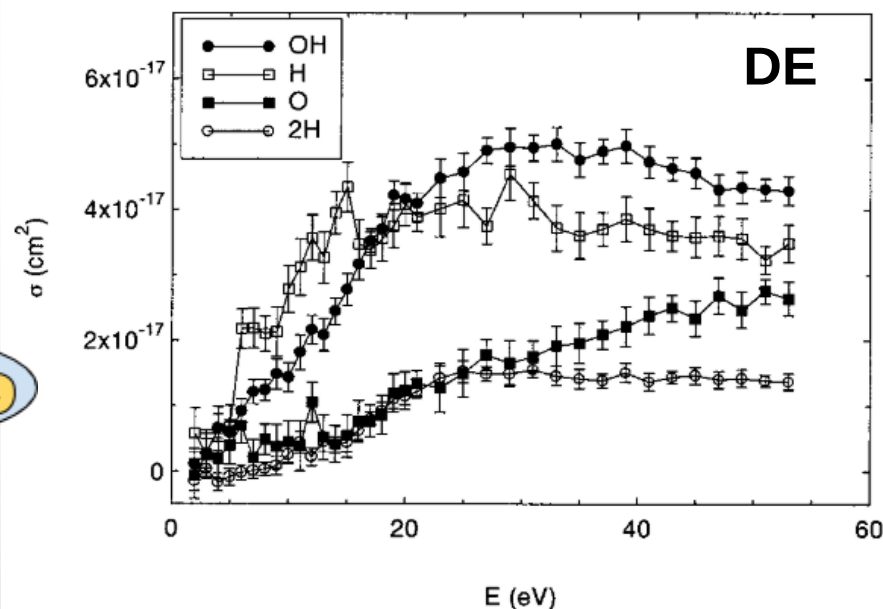


H₂O⁺: dissociative excitation

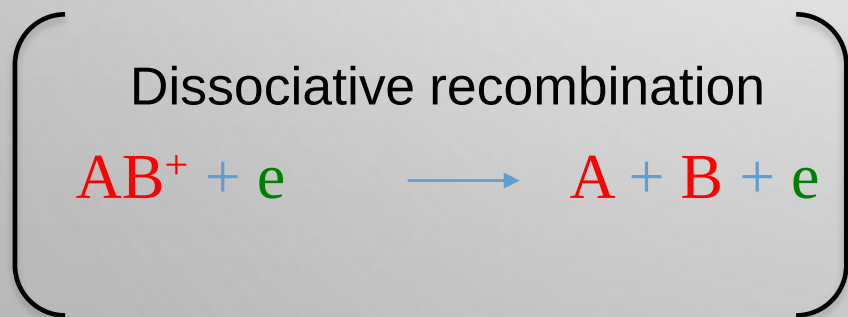
Dissociative excitation



Storage ring measurements of DE and DR



Jensen et al, PRA **60** (1999) 2970



Complexity similar to DR

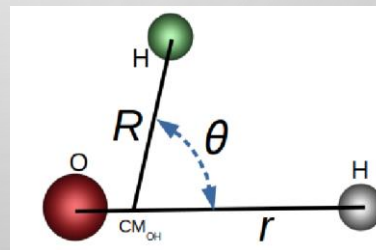
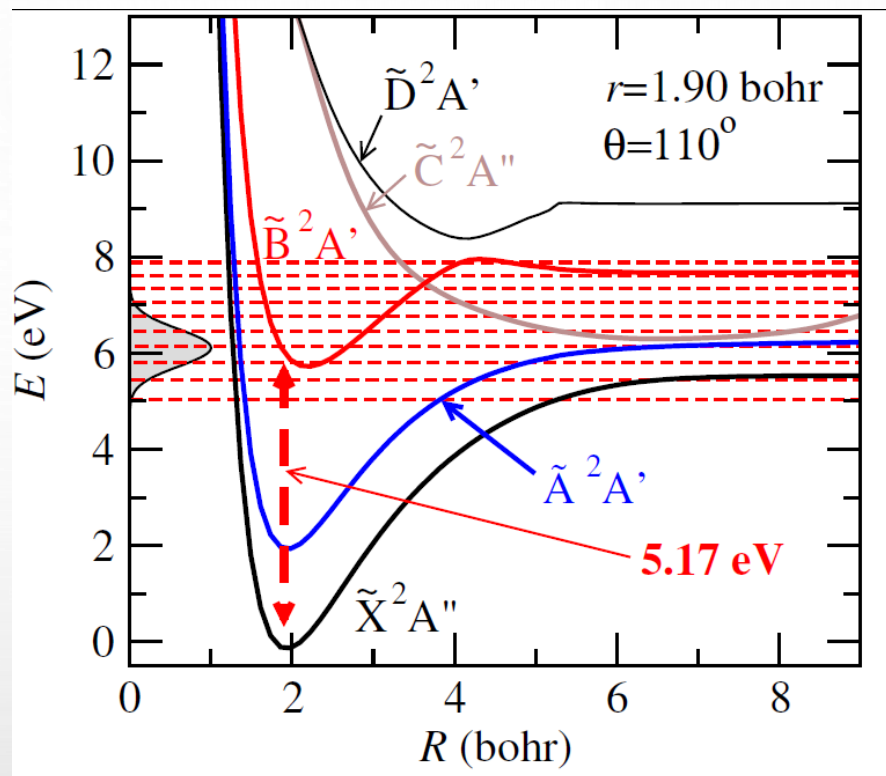
Rabadan and Gorfinkiel, PRA **103** (2021) 012808

H_2O^+ : dissociative excitation (DE)

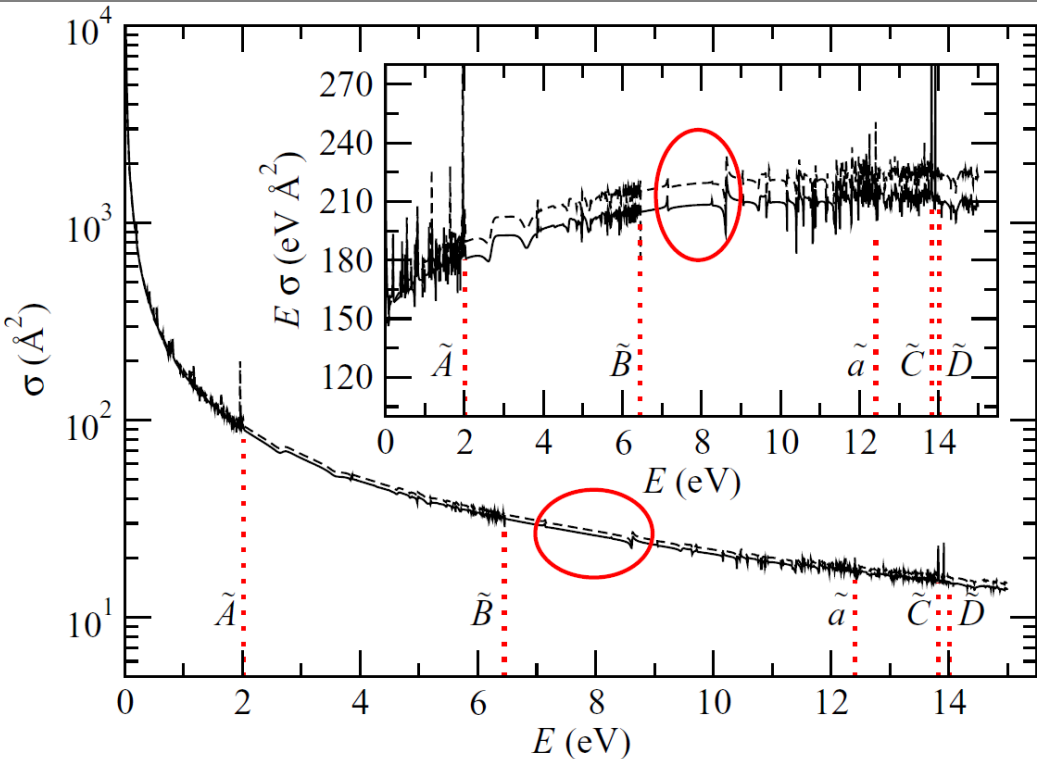
Possible 'routes':

- Excitation into electronic (pre)dissociative state
- Excitation into vibrational continuum of bound electronic state
- Coupling between electronic states
- Excitation into resonant state that decays into a dissociative state
- Excitation into dissociative resonant state (followed by detachment)

d and e normally compete and outcome (DE/DR) depends on resonance lifetime among other things.



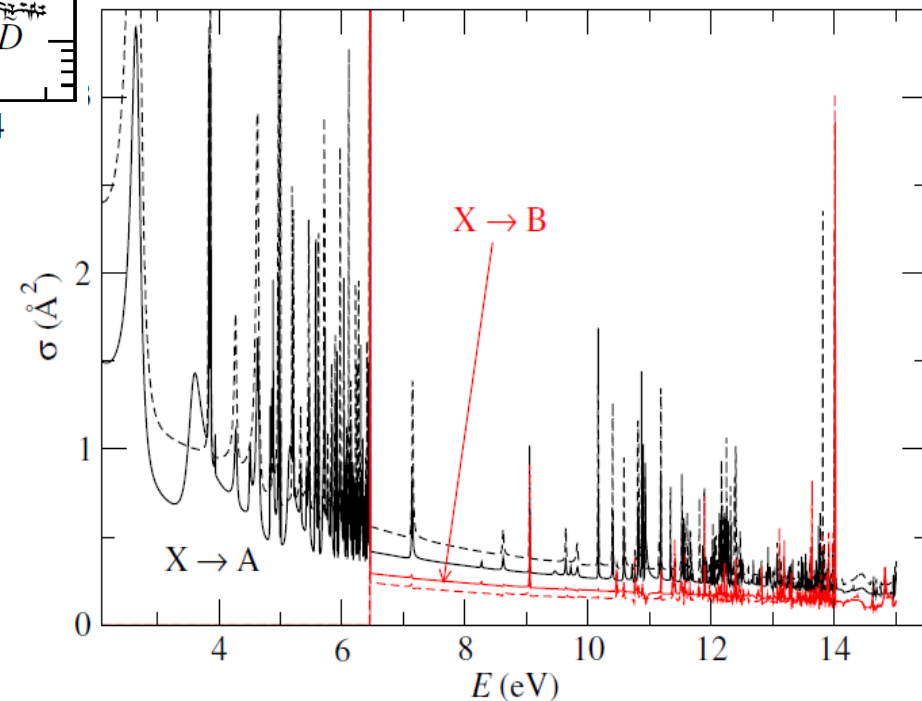
H₂O⁺: elastic and inelastic scattering



Elastic cross section

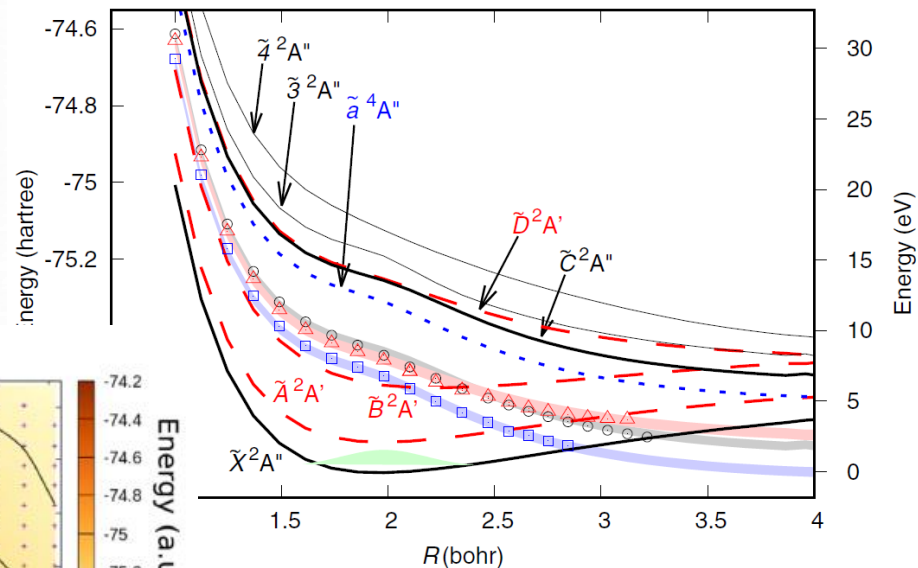
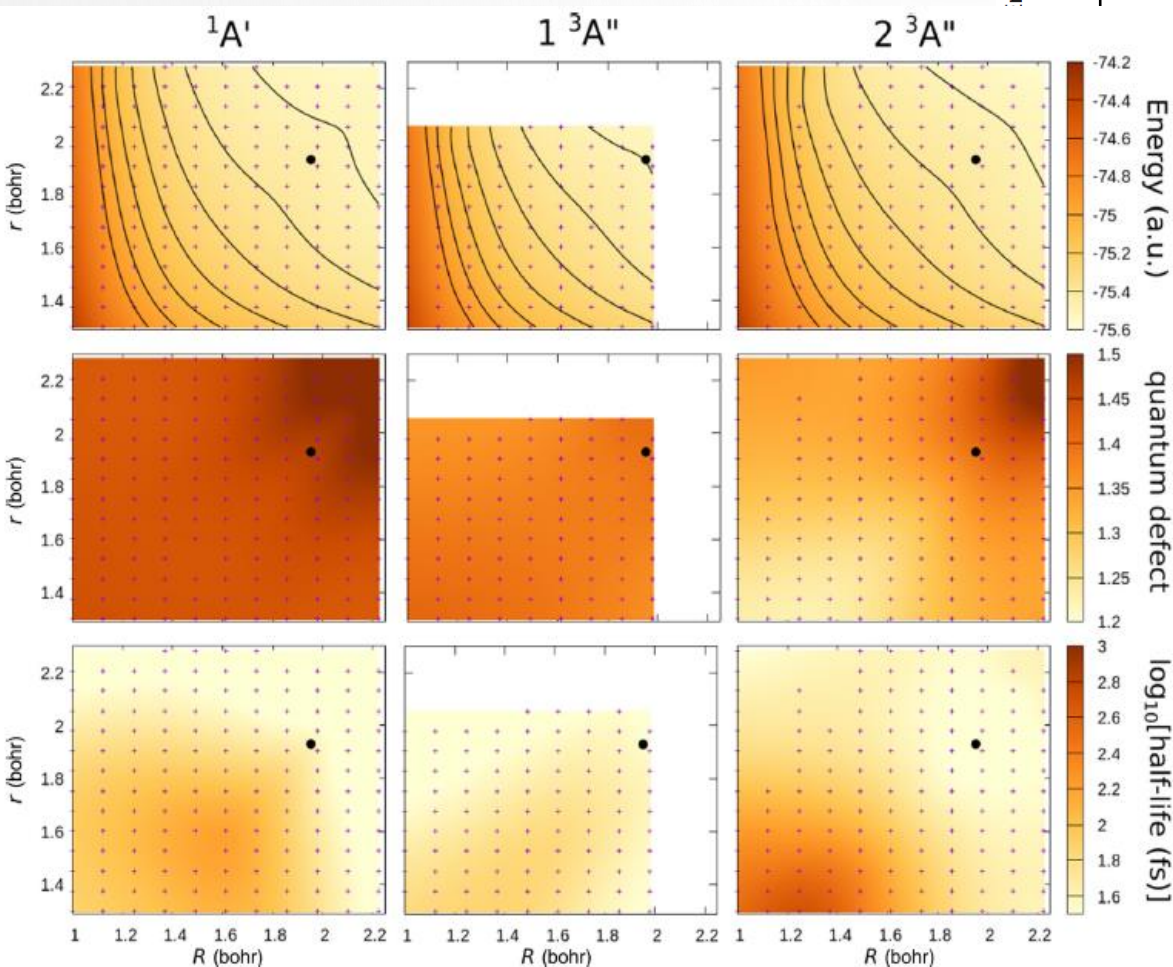
Excitation into the first and second electronic states

H₂O⁺ present in biomedical plasmas, Saturn's inner plasma disk, other astrophysical environments, etc.



H₂O⁺: towards DE

Large number of resonances
decaying to B state: effect on DE?
Study of 3 'dissociative' resonances.



Investigated survival
probability resonances
above B state: resonance
lifetimes vs. '1D
dissociation time' for DR
seem to indicate DR is
more likely than DE...

Interatomic Coulombic electron capture

Environment enabled process

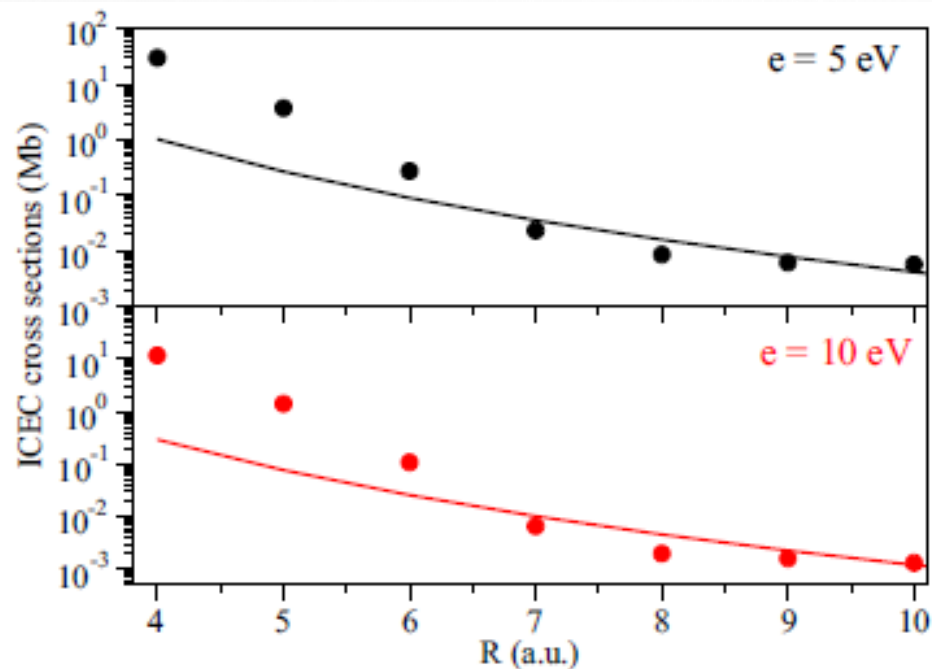
$e + \text{Ne}^+ \rightarrow \text{Ne}^+ + e$ elastic/inelastic scattering

$e + \text{Ne}^+ @ \text{He}_n \rightarrow \text{Ne} @ \text{He}_n^+ + e$ **capture**

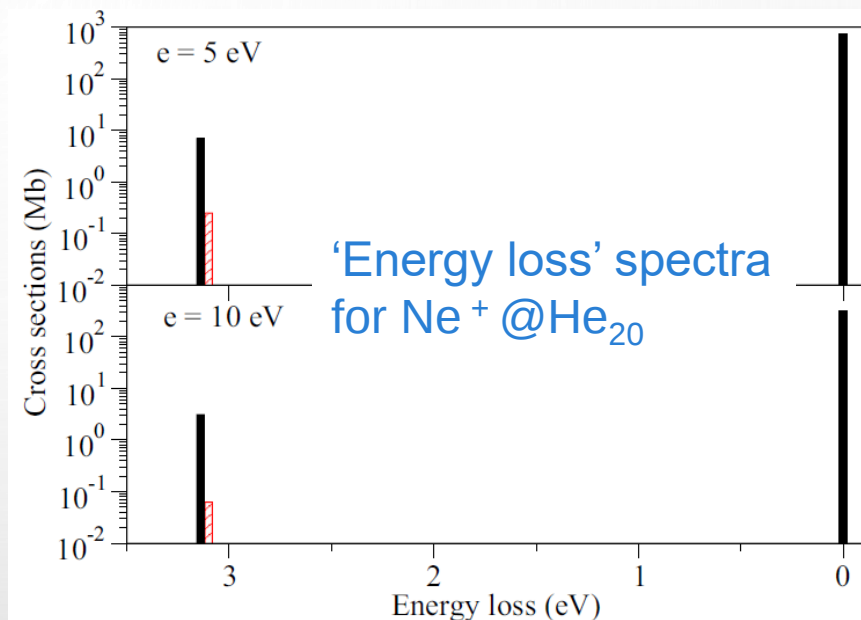
IP Ne: 21.56 eV < IP He: 24.59 eV $\rightarrow$ no 'spontaneous' electron transfer

If KE of projectile > ~ 3 eV $\rightarrow$ ionization of He is possible

Interatomic Coulombic electron capture



R: Ne-He distance (circles, calculated; lines, predicted)



$\text{Ne}^+ @ \text{He}_{20}$: 2000 geometries obtained from a MonteCarlo approach and then a sum over all Ne^+ -He pairs for each

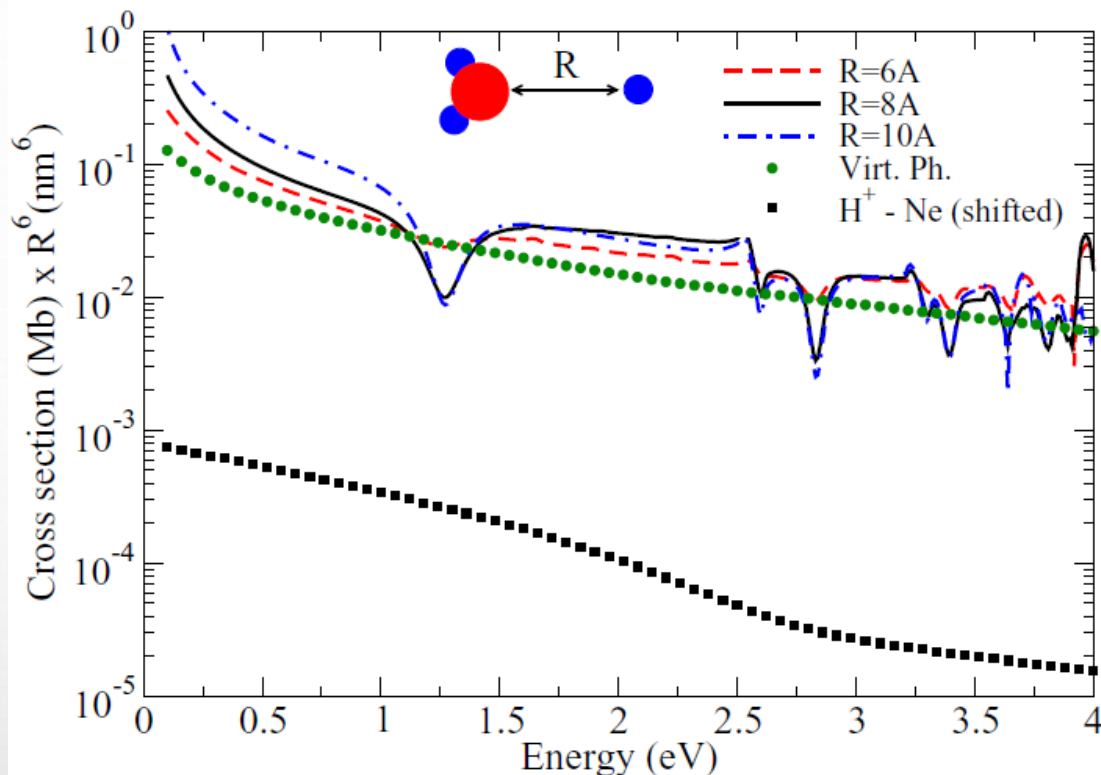
ICEC/elastic cross section ratio $\approx 10^{-2}$

Inelastic/elastic cross section ratio, measured by EELS $\approx 2 \cdot 10^{-2}$ (e.g. pyrimidine)

Interatomic Coulombic electron capture



Spin	Sym.	E (eV)	State
Singlet	B_1	0.0	$\text{H}(1s)\text{-H}_2\text{O}^+(1b_1^{-1})$
Triplet	B_1	0.0	$\text{H}(1s)\text{-H}_2\text{O}^+(1b_1^{-1})$
Singlet	A_1	2.29	$\text{H}(1s)\text{-H}_2\text{O}^+(3a_1^{-1})$
Triplet	A_1	2.29	$\text{H}(1s)\text{-H}_2\text{O}^+(3a_1^{-1})$
Singlet	A_1	2.50	$\text{H}^+\text{-H}_2\text{O}(\tilde{X})$
Singlet	B_2	6.66	$\text{H}(1s)\text{-H}_2\text{O}^+(1b_2^{-1})$
Triplet	B_2	6.66	$\text{H}(1s)\text{-H}_2\text{O}^+(1b_2^{-1})$
Triplet	B_1	9.29	$\text{H}^+\text{-H}_2\text{O}^*(^3B_1)$
Singlet	B_1	9.95	$\text{H}^+\text{-H}_2\text{O}^*(^1B_1)$
Triplet	A_1	11.93	$\text{H}^+\text{-H}_2\text{O}^*(^3A_1)$
Singlet	A_1	12.85	$\text{H}^+\text{-H}_2\text{O}^*(^1A_1)$
Triplet	B_1	14.70	$\text{H}(1s)\text{-H}_2\text{O}^+(^4B_1)$
Triplet	B_2	15.49	$\text{H}^+\text{-H}_2\text{O}^*(^3B_2)$
Triplet	B_1	15.74	$\text{H}^+\text{-H}_2\text{O}^*(^3B_1)$
Singlet	B_1	15.74	$\text{H}^+\text{-H}_2\text{O}^*(^1B_1)$
Singlet	A_1	15.87	$\text{H}^+\text{-H}_2\text{O}^*(^1A_1)$
Triplet	A_1	15.87	$\text{H}^+\text{-H}_2\text{O}^*(^3A_1)$
Singlet	B_2	16.69	$\text{H}^+\text{-H}_2\text{O}^*(^1B_2)$



ICEC cross section enhanced/supressed due to the presence of resonant neutral states

The presence of a cation near the molecules substantially changes the scattering processes

Conclusions

- Electronically elastic and inelastic integral and differential cross sections can be calculated *ab initio* for:
 - small and mid-size molecules.
 - lower excited states
 - up to ~15-20 eV
- Break-up (dissociative excitation) harder to model: **work in progress.**
- ‘Novel’ process like ICEC have hardly been explored but could be significant.

Collaborators



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al., Paris, France

Software development: UCL, Charles University Prague, STFC, MBL, etc.

